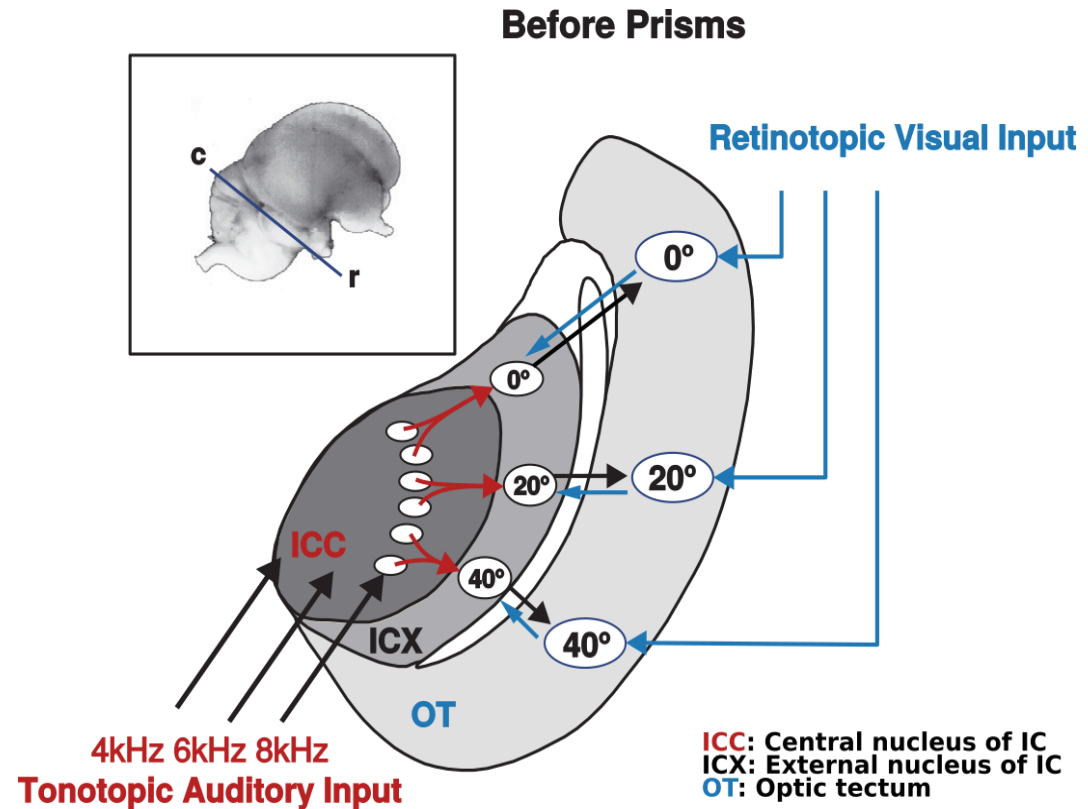


Computational Investigation of Visually Guided Learning of Spatially Aligned Auditory Maps in the Colliculus

Timo Oess, Marc O. Ernst, Heiko Neumann

Aligning Auditory Maps of Space

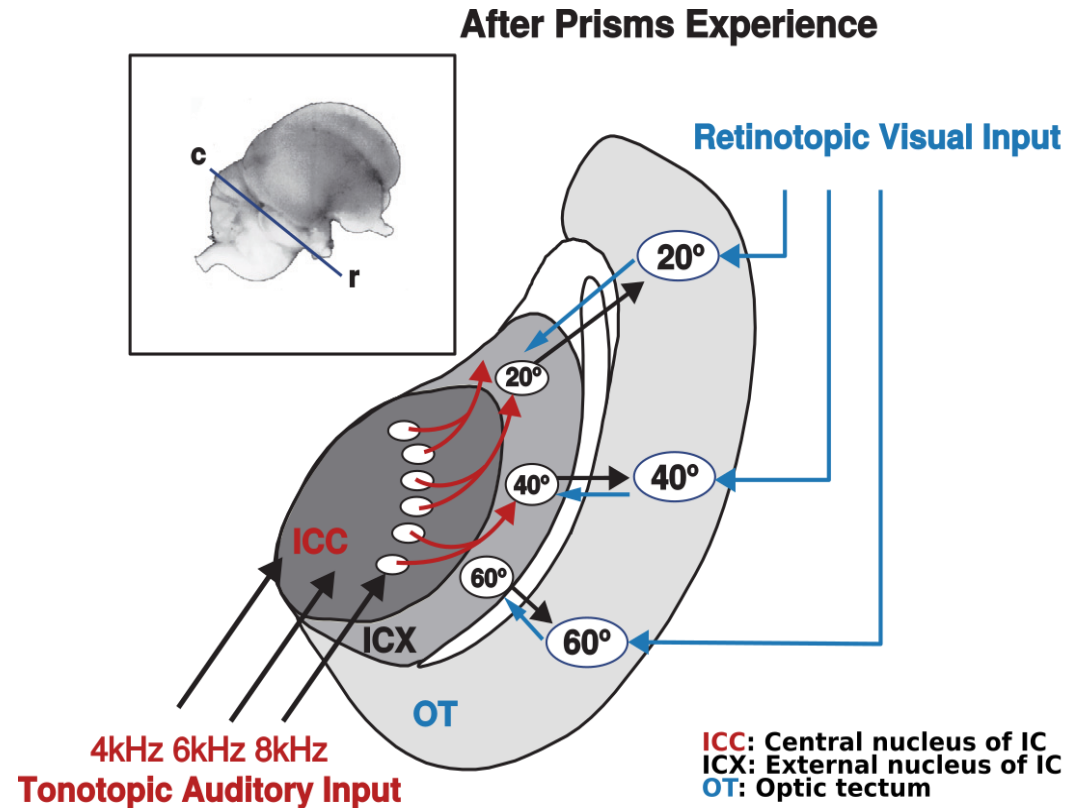
- Sensory receptor surface for auditory inputs is tonotopically organized.
- Spatial location of a sound source derived from computed binaural cues.
- Association between cues and spatial locations needs to be learned.
→ Vision serves as a guidance signal



Adapted from Pena, J. L., & Gutfreund, Y. (2014) Current opinion in neurobiology
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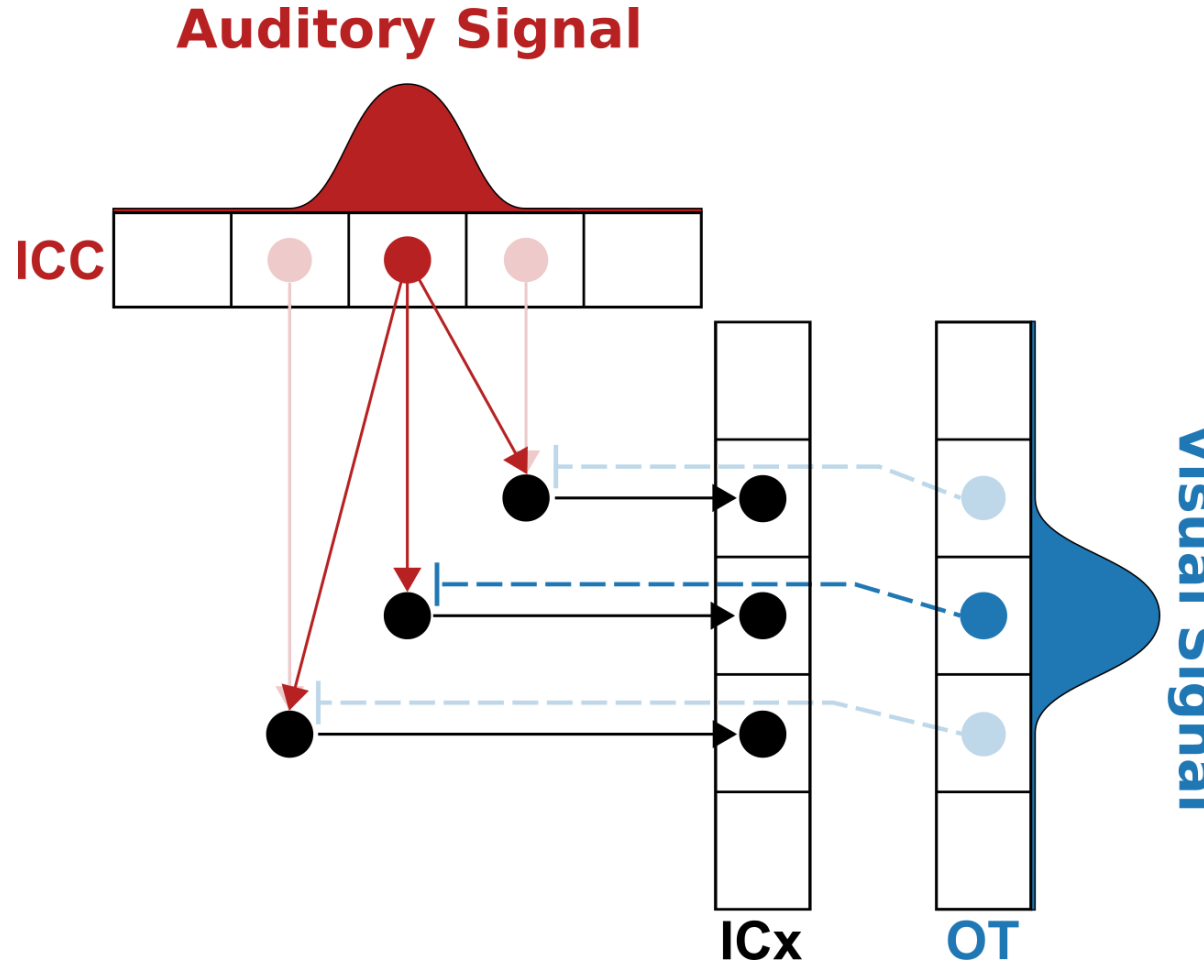
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Model Implementation

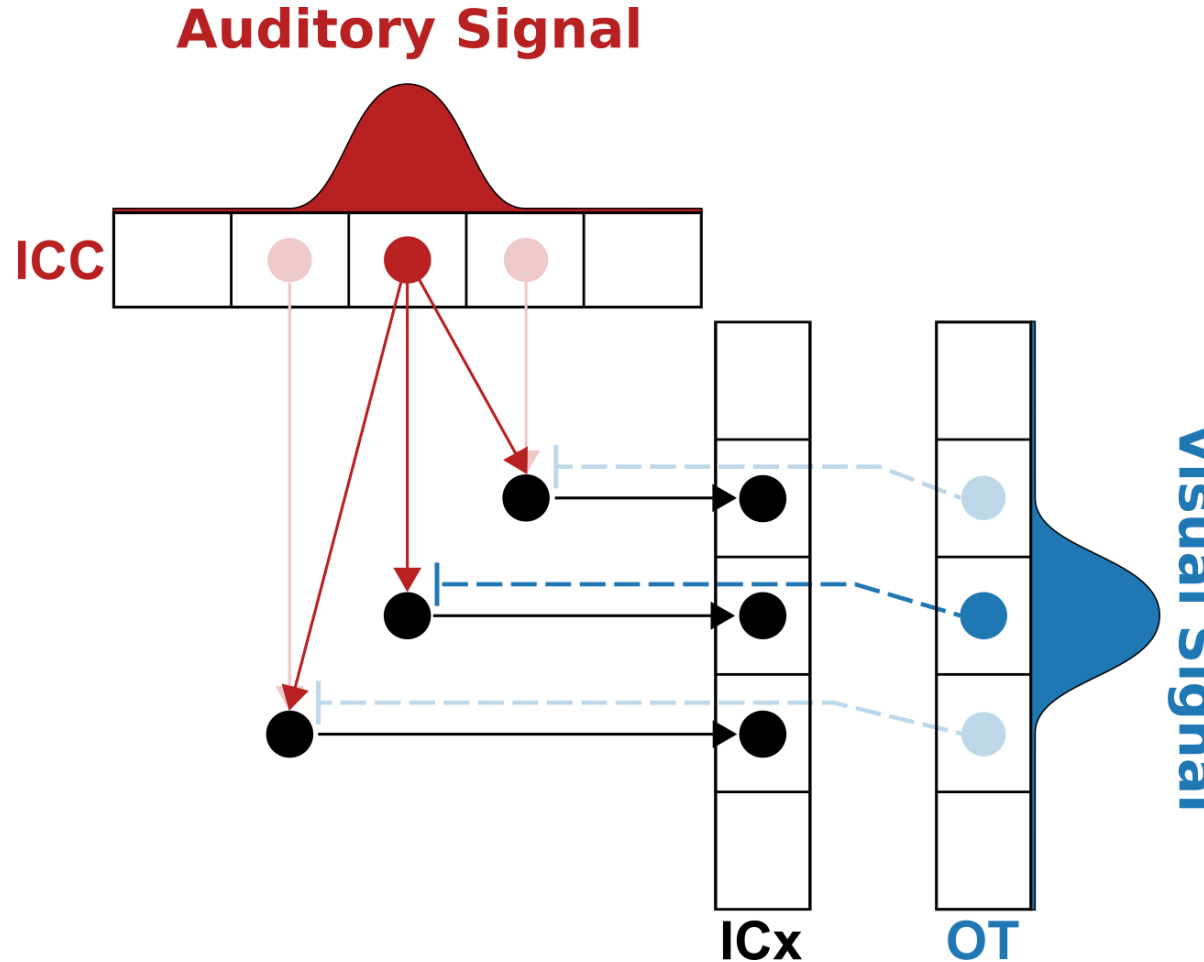
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Gerstner et. al (2018) *Frontiers in Neural Circuits*
Oja, E (1989) *International Journal of Neural Systems*

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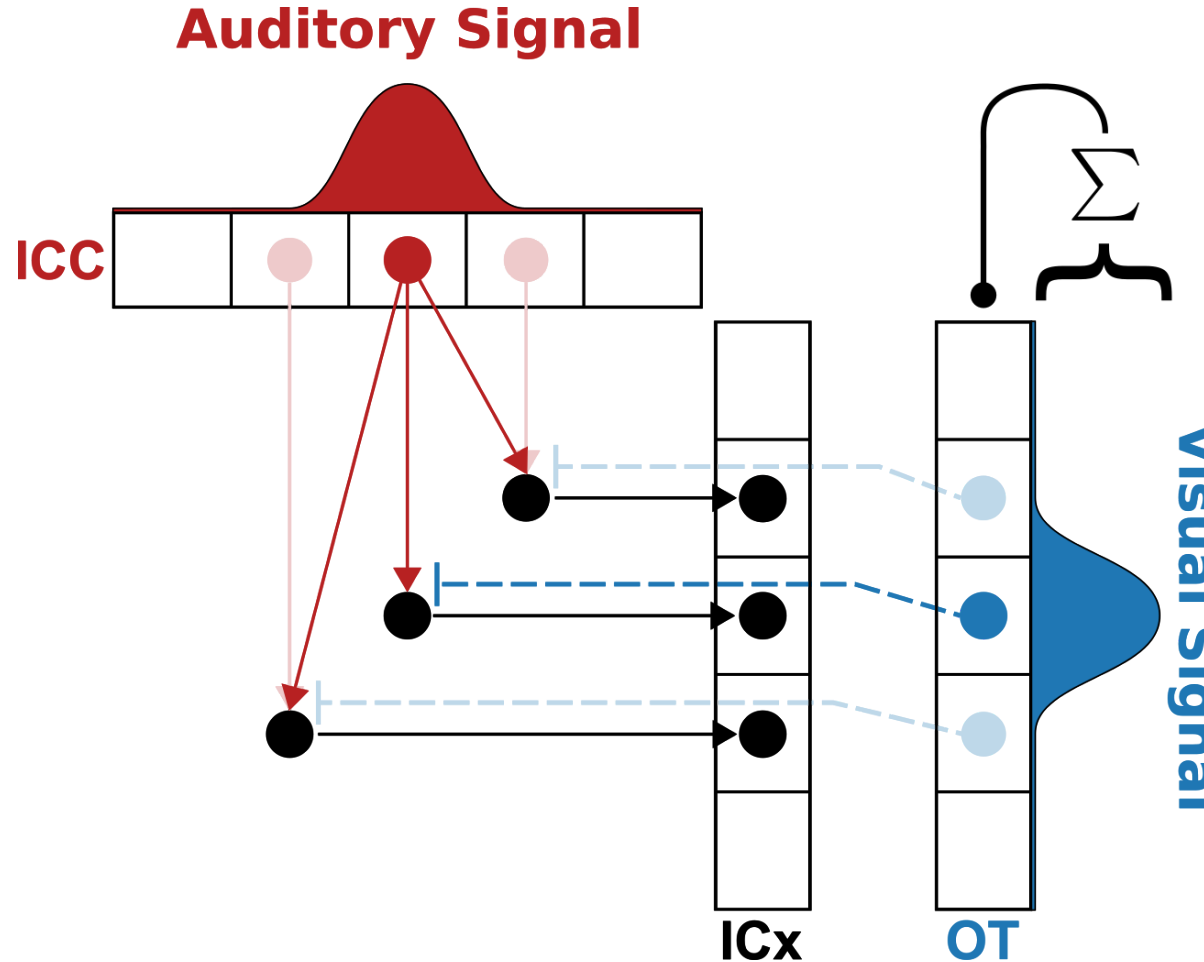
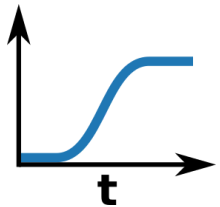


Gerstner et. al (2018) *Frontiers in Neural Circuits*

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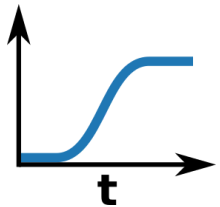


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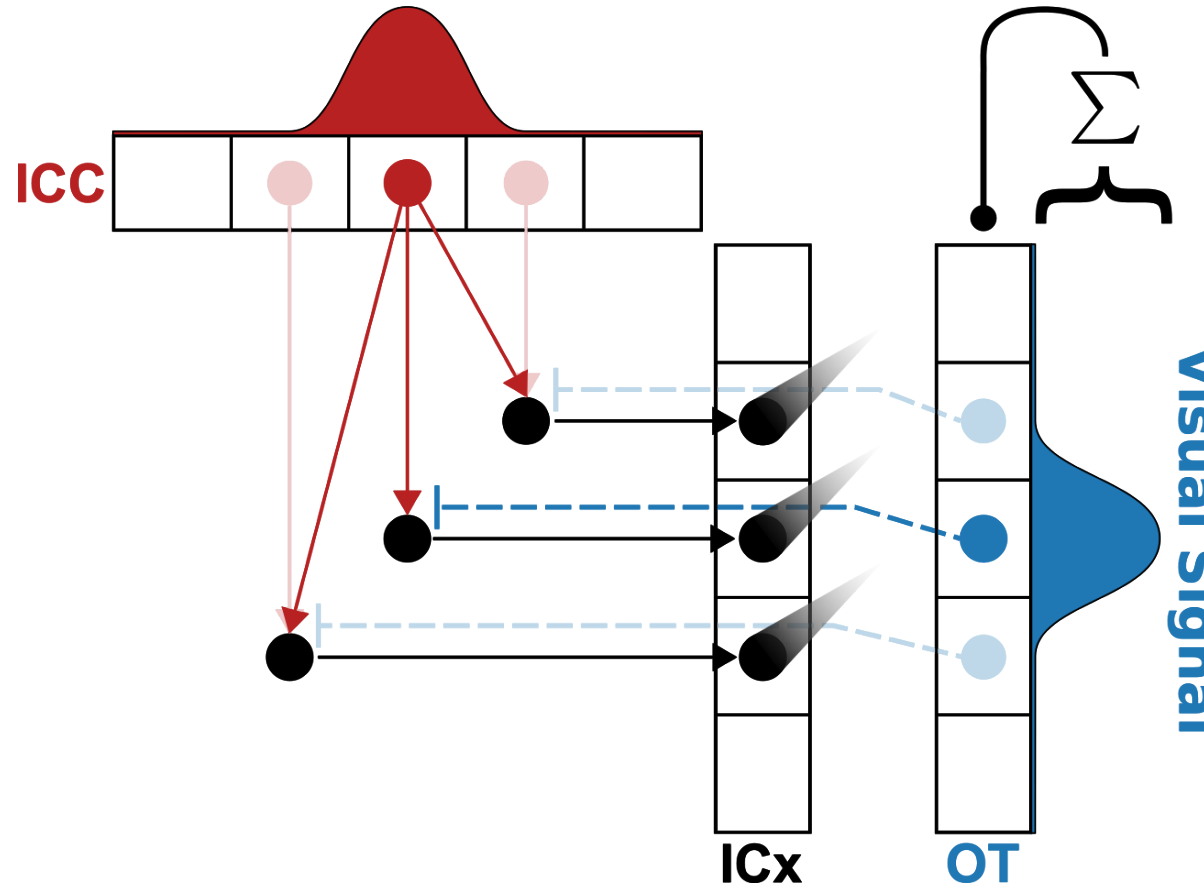
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- **Temporal Trace**: improves learning of temporally shifted signals

Auditory Signal

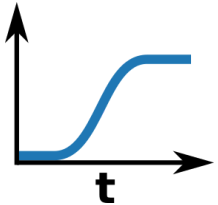


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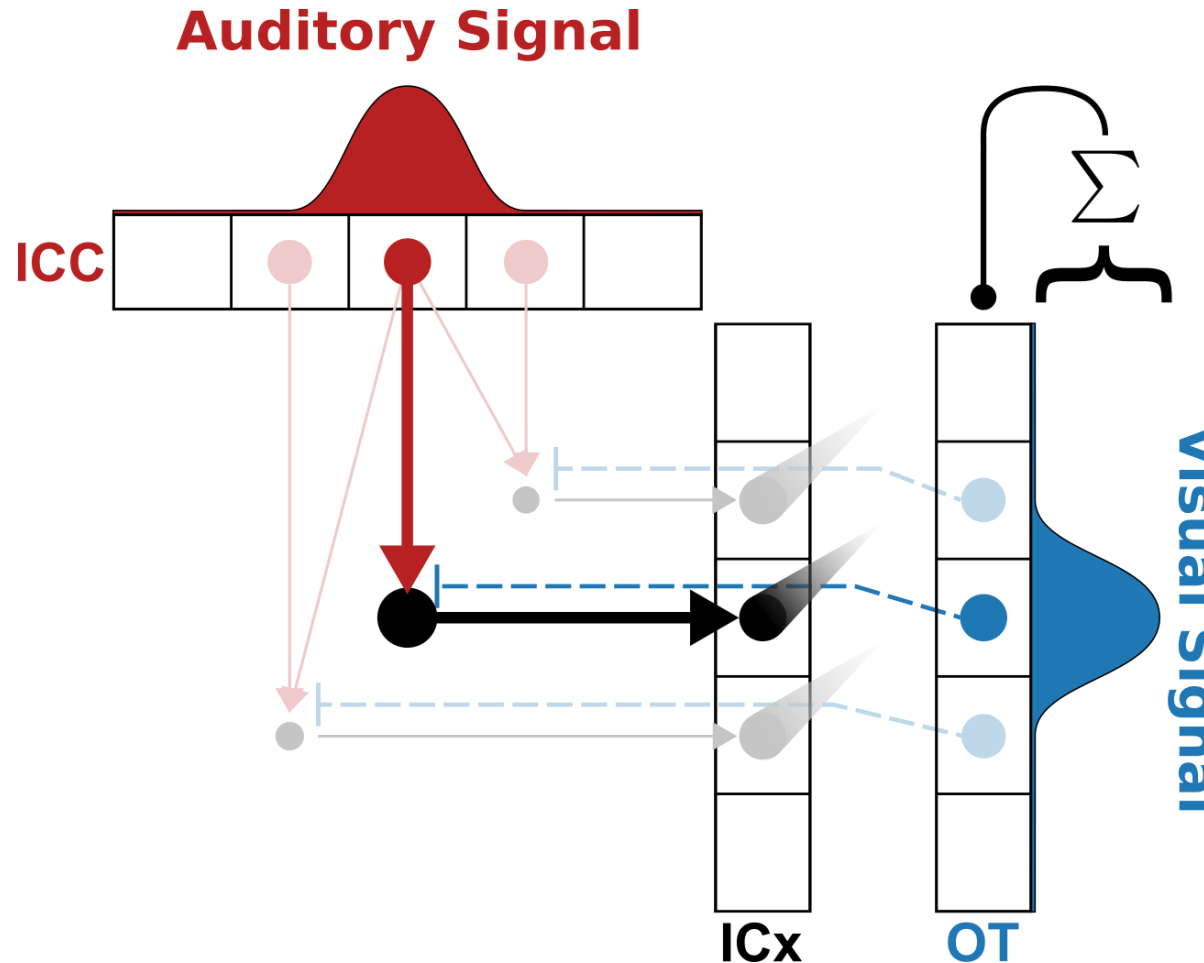
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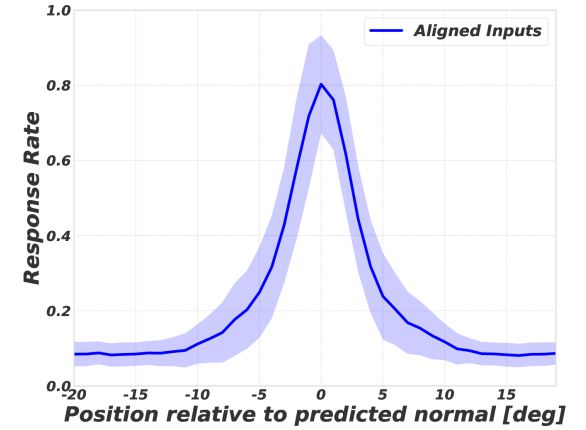
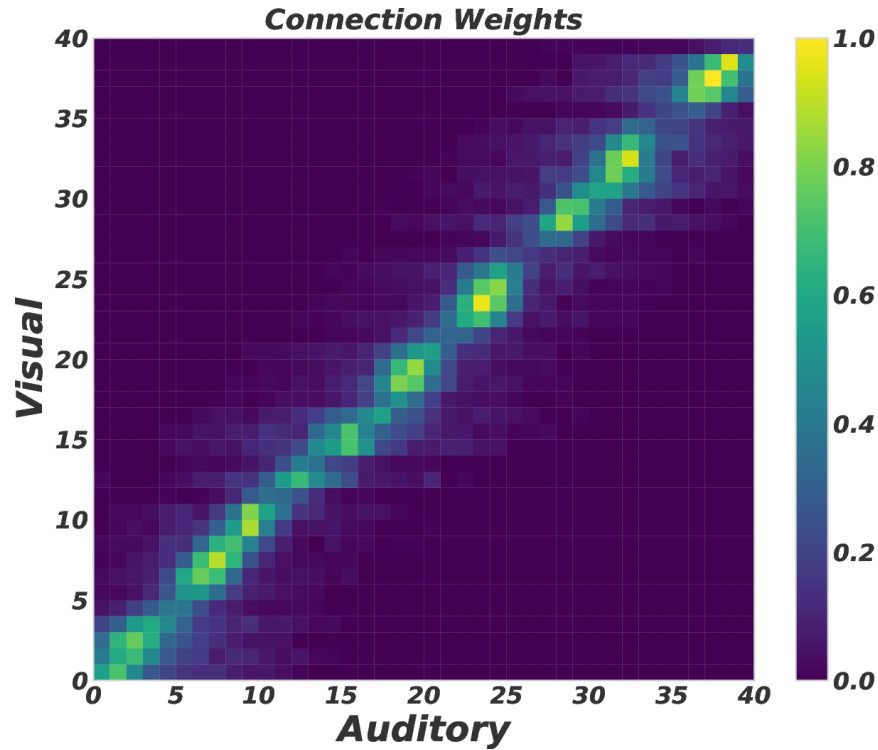
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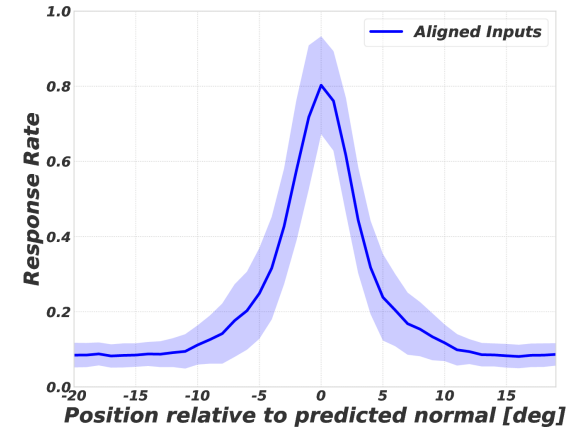
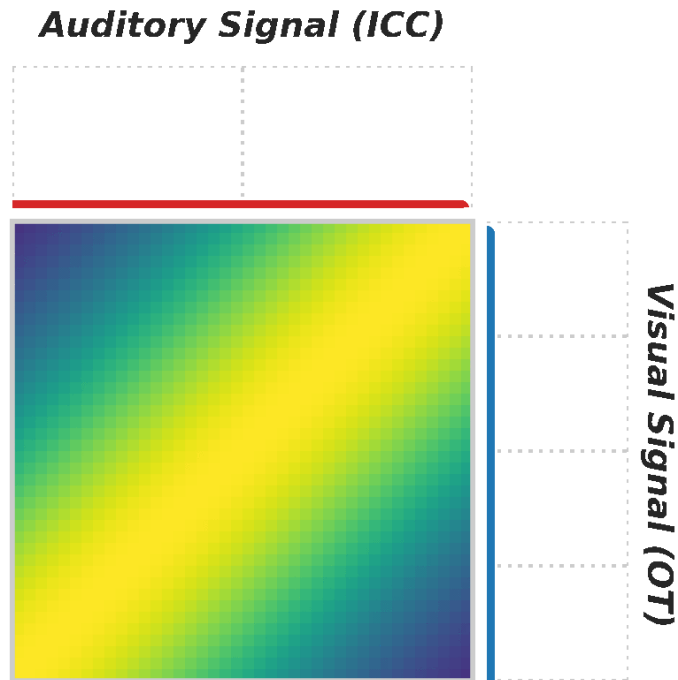
Results - Default Inputs

- Vision and audio inputs spatially aligned
- Temporal coincidence of stimuli
- Successful alignment of maps



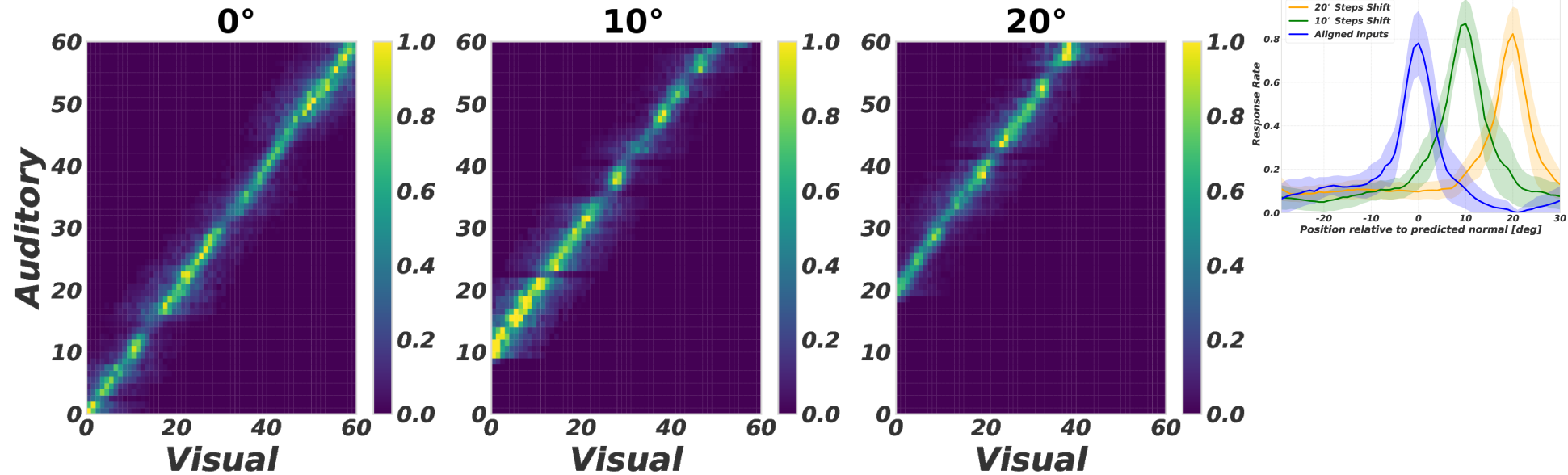
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Results - Prismatic Shift during rearing

- Visual input is prismatically shifted with different offsets (Rearing barn owls with a prismatic shift [Knudsen1989])
- Auditory map alignment shifts according to visual shift (0°, 10°, 20°)



Knudsen, E. I. and Knudsen, P. F. (1989) Journal of Neuroscience

Results - Prismatic Shift in Adult Owls

- “Incremental training increases the plasticity of the auditory space map in adult barn owls”
[Linkenhoker2002]
- Single large prismatic (visual) shift does **not** induce a shift but unlearning. Shift of auditory map possible with incremental steps.

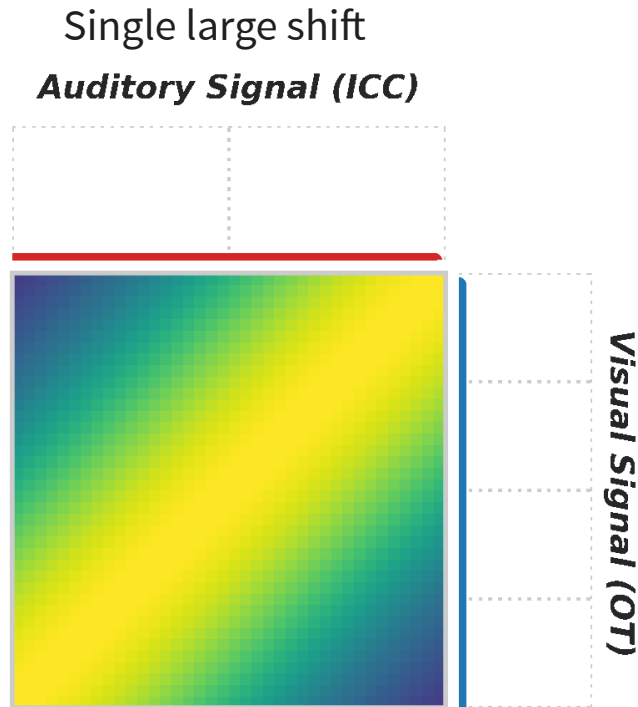
Single large shift

Incremental shifts

Linkenhoker, B. A. and Knudsen, E. I. (2002) Nature

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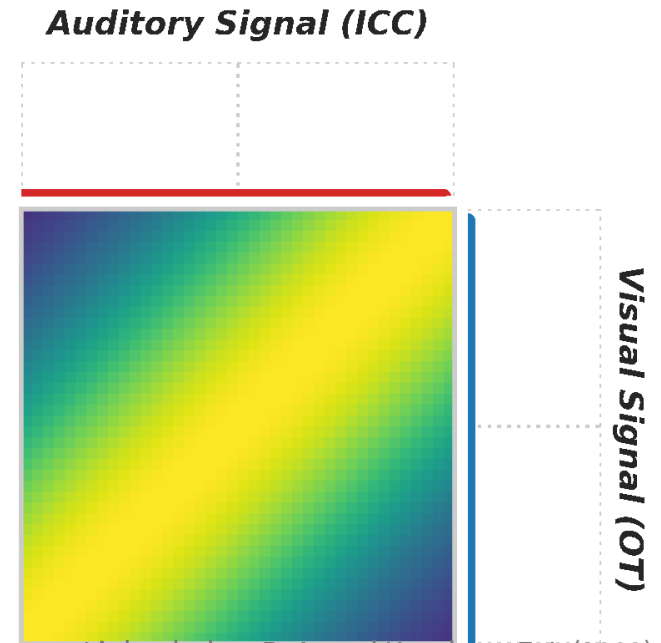
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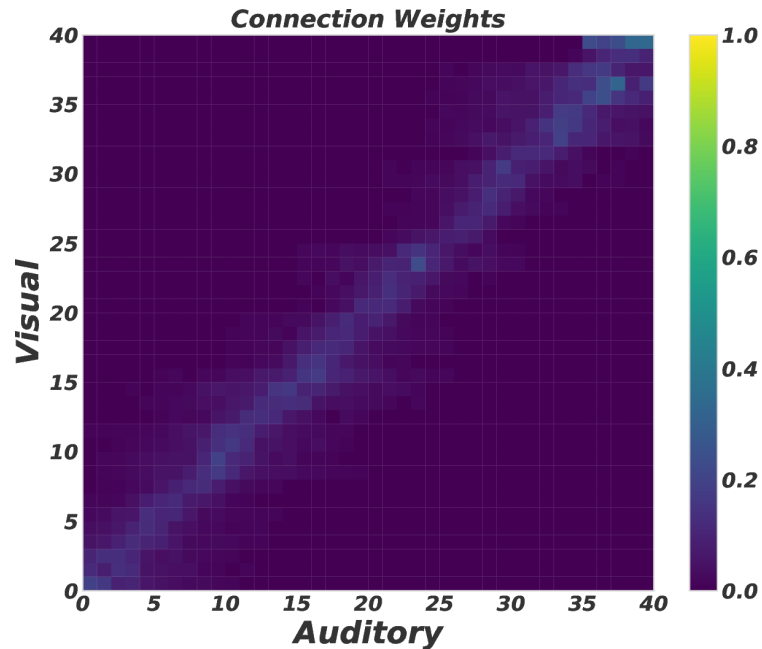


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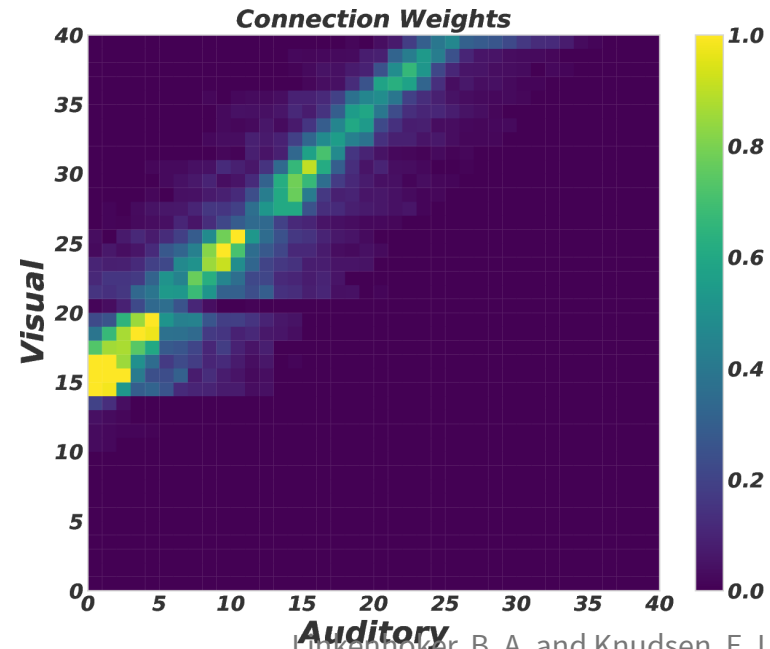
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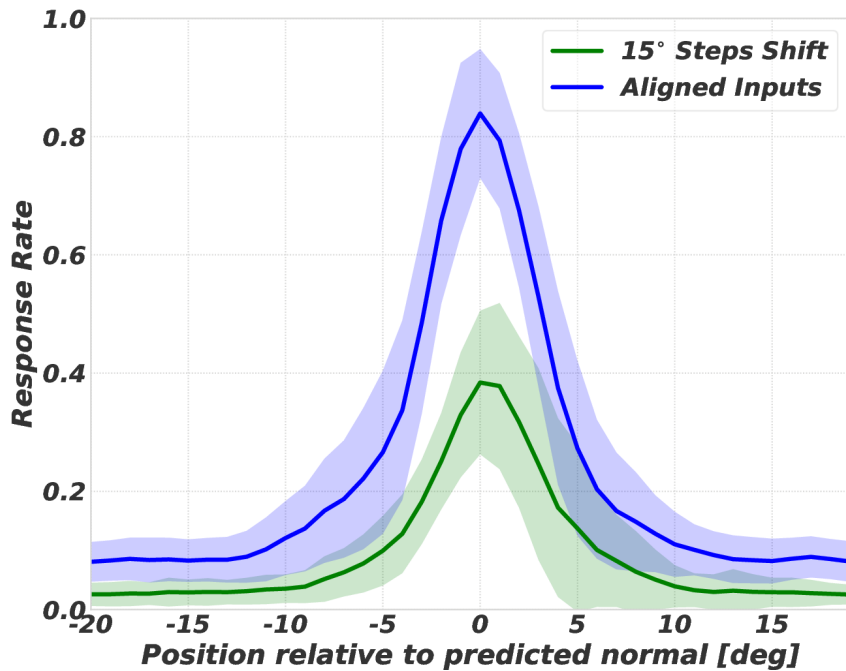


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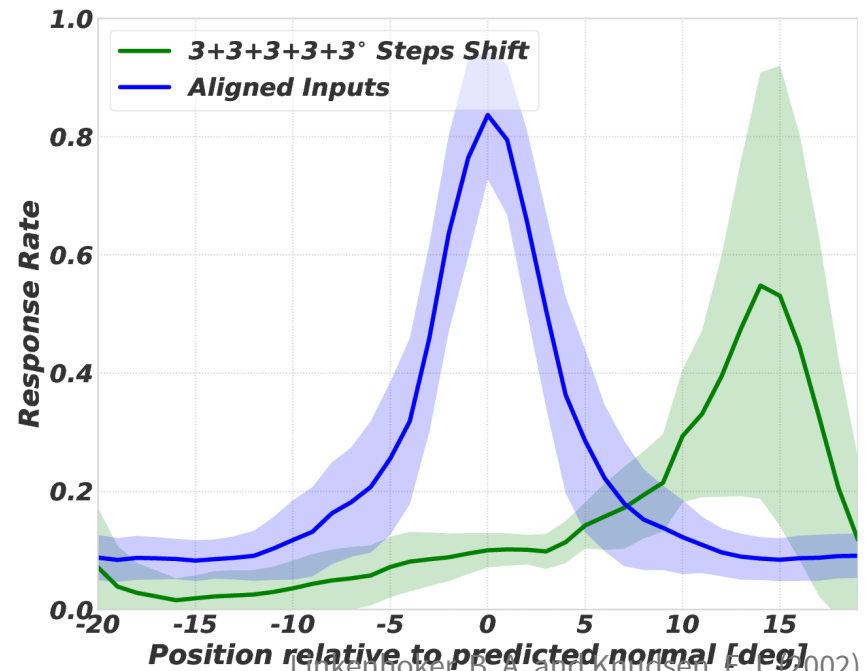
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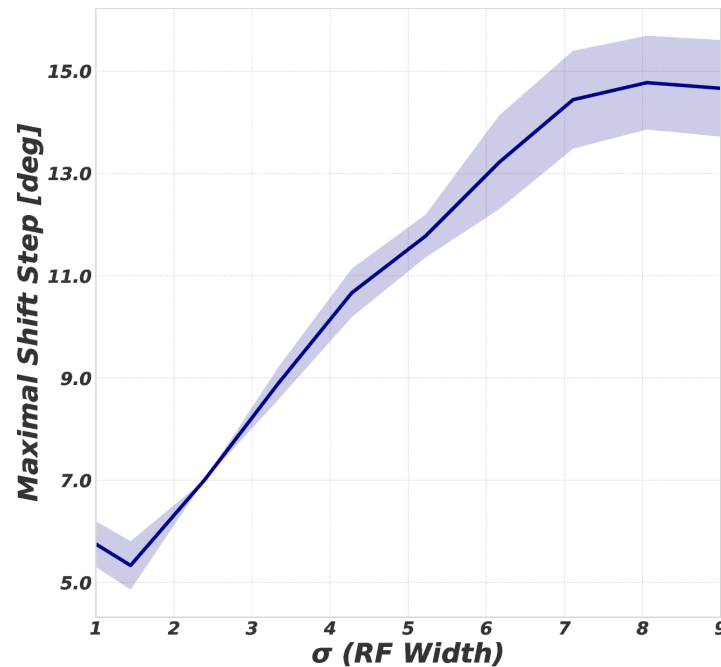


Linkenhoker, B. A. and Knudsen, E. F. (2002) Nature

Results - Model Prediction

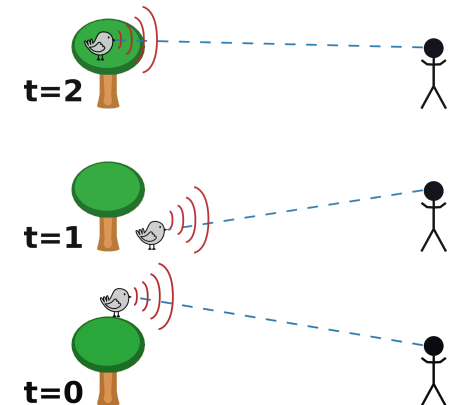
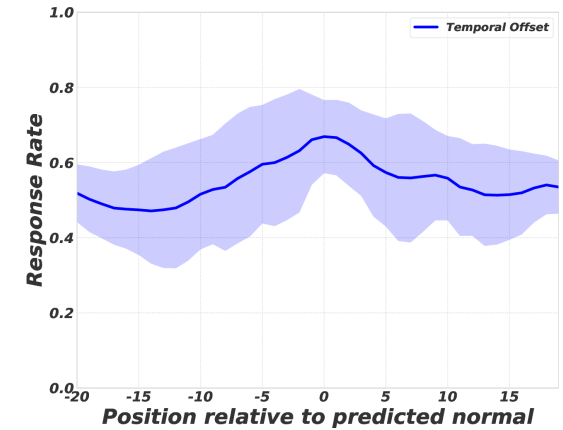
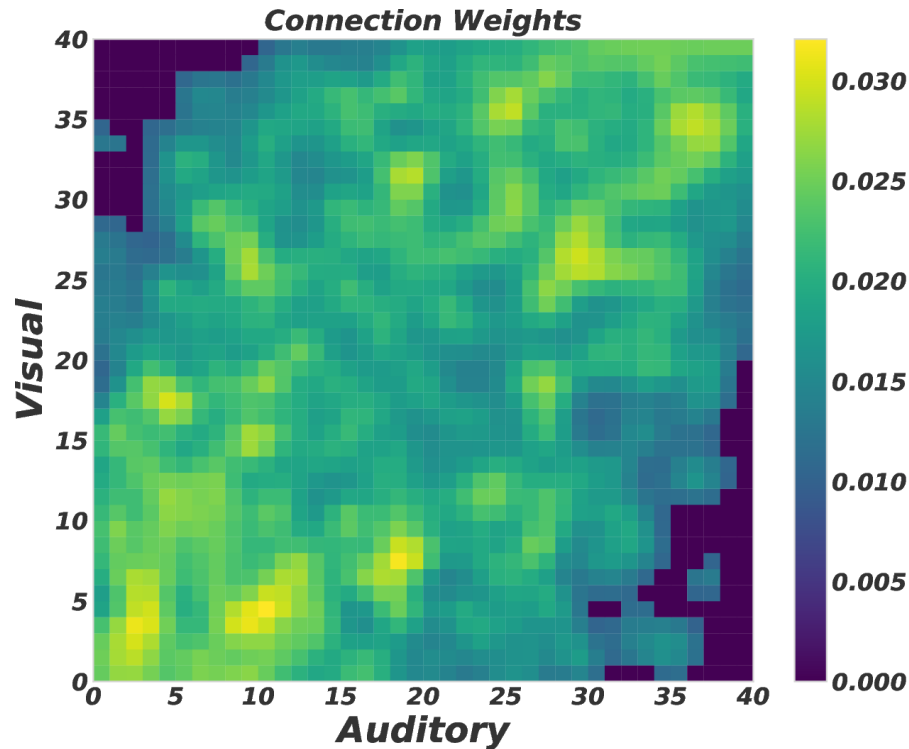
Ability to shift the alignment of the auditory map correlates with the receptive field size of the auditory map neurons.

- Receptive field size large at learning onset
 - Gradually shrinks until adult state is reached
- Hypothesis: Relearning is only possible if shifted visual stimulus is still within receptive field of auditory neuron



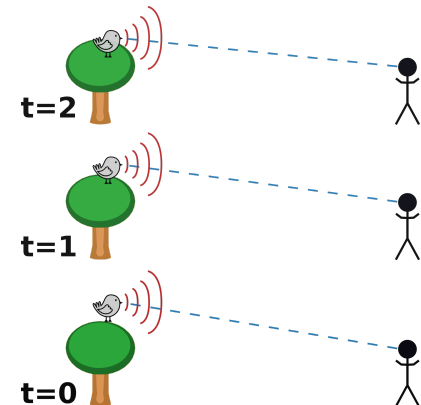
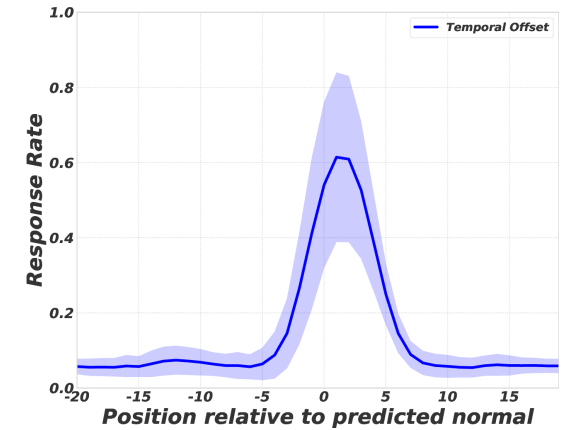
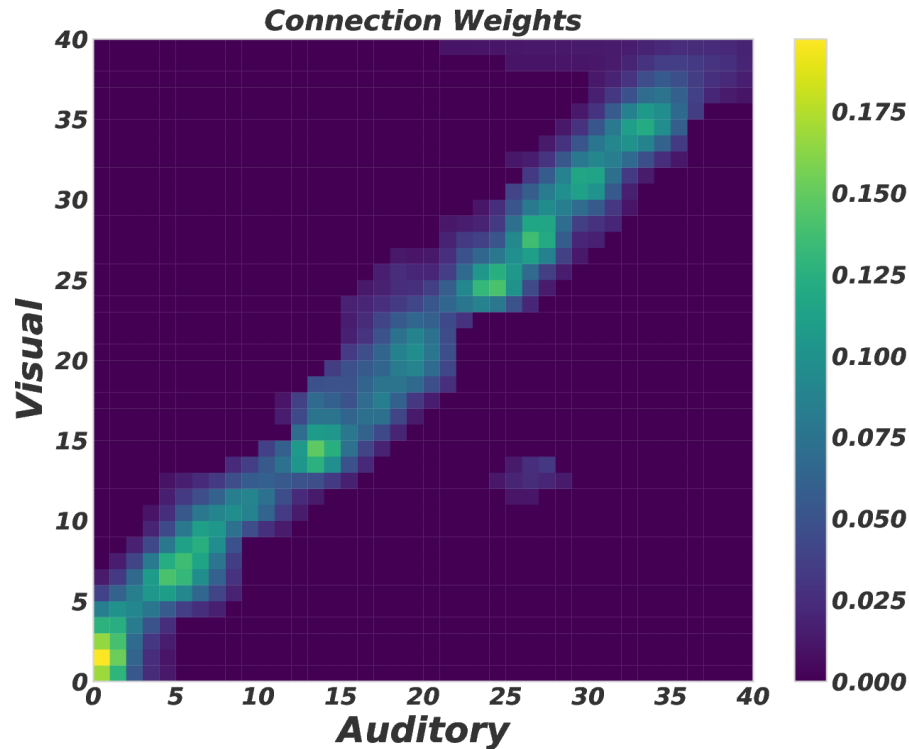
Results - Temporally Shifted Inputs (1/3)

- Visual and auditory inputs are temporally shifted
- Stimulus locations are randomly chosen from a uniform distribution
→ **Low** autocorrelation of stimulus locations



Results - Temporally Shifted Inputs (2/3)

- Visual and auditory inputs are temporally shifted
- Stimulus locations are randomly chosen from a Wiener process
→ High autocorrelation of stimulus locations

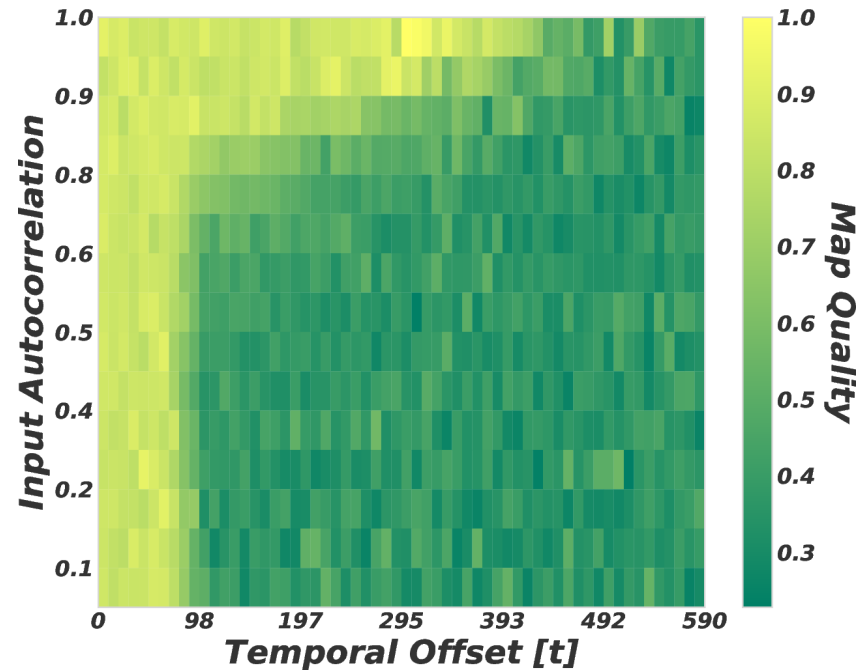


Results - Temporally Shifted Inputs (3/3)

Quality of map alignment depends on spatio-temporal correlation of inputs.

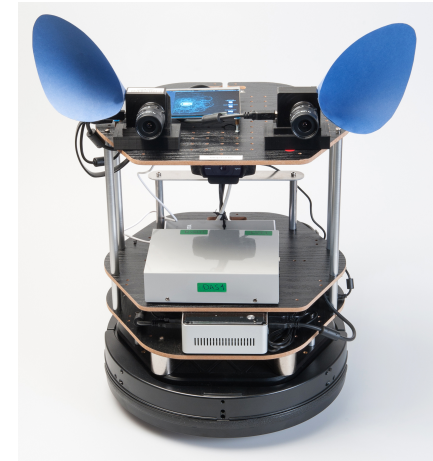
- Temporal coincidence is crucial for stimuli with low autocorrelation of stimulus locations
- Highly autocorrelated stimulus locations lead to successful map alignment even for large temporal offsets

→ Learning depends on the spatial autocorrelation of the inputs



Conclusion

- Ability of shifting auditory map in adult animals depends on the receptive field size of auditory neurons.
 - Large Receptive Fields → Large shifts are possible
 - Small Receptive Fields → Small, gradual shifts are need
- Spatial autocorrelation of inputs
 - Temporal offset between stimuli effects learning
 - Map alignment is still possible for highly autocorrelated inputs
- Model allows flexible and stable map formation
 - Suitable for real-world application in mobile robots



Thank you

Model Implementation - Equations

- Conductance based neuron population of ICx:

$$\tau \dot{r}_j = -\alpha \cdot r_j + (\beta - r_j) \cdot \sum_{j=0}^N w_{ji} \cdot s_i^A$$

- Randomly initiated connection creation.
- 3-Component-Learning-Rule [Gerstner2018]:

$$\Delta w_{ji} = \eta \cdot ((post_j(t) \cdot pre_i(t) \cdot fb_j(t) - stab_j(t)))$$

with:

$$post_j(t) = \bar{r}_j(t)$$

$$pre_i(t) = s_i^A \text{ (auditory input)}$$

- Temporal Trace:**

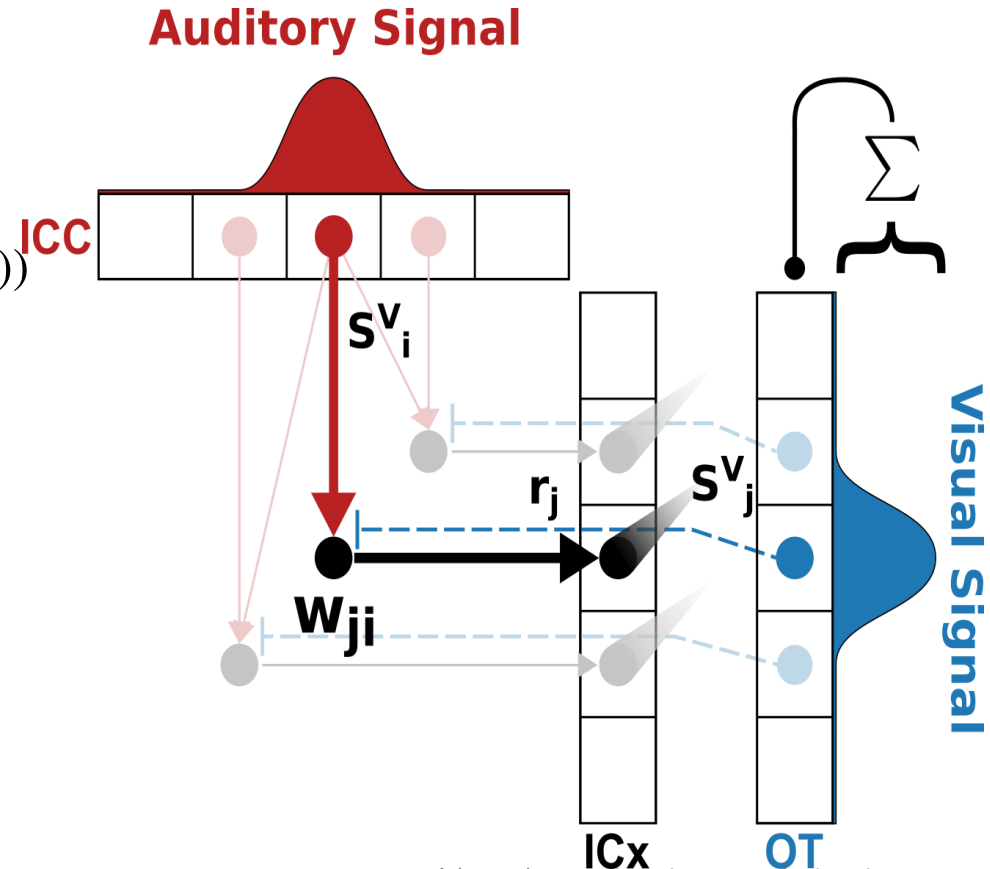
$$\bar{r}_j(t + \delta t) = (1 - \lambda) \cdot \bar{r}_j(t) + \lambda \cdot r_j(t)$$

- Eligibility (Controlled by Vision):**

$$fb_j(t) = \hat{s}_j^V(t) \cdot E(t)$$

- Stabilizer (leads to [Oja1989]):**

$$stab_j(t) = \bar{r}_j^2 \cdot w_{ji}$$



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